

Ch. 2 - Measurement & Stats

- [2-day version]

131

Psychology 402 - Spring 2024 - Dr. Michael Diehr

Copyright © 2024 Michael Diehr
All Rights Reserved

For use only by students enrolled
in my sections of Psyc 402
through the end of the semester.
May not be posted, shared or uploaded
online without permission.

132

Psychology 402 - Spring 2024 - Dr. Michael Diehr

$$S = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N - 1}}$$

134

Psychology 402 - Spring 2024 - Dr. Michael Diehr

Measurement & Stats

- Day 1
 - Measurement Scales
 - Why numbers?
 - Distribution & Graphs : Histogram
 - Central Tendency
 - Mean, SoR, SSR, Variance, Standard Deviation
 - Start Exercise 1
- Day 2
 - Population vs. Sample
 - Precision vs. Accuracy
 - Logic and Logical Fallacies
 - Percentile Rank, Norms
 - Z-score exercise (in class)

135

Psychology 402 - Spring 2024 - Dr. Michael Diehr

Measurement Scales

- Nominal
- Ordinal
- Interval
- Ratio

136

Psychology 402 - Spring 2024 - Dr. Michael Diehr

Nominal Scale

- Nominal: Name or ID only
 - red, blue, green....
john, tony, fred...
Sci2-243, Sci2-245...
 - does not signify Ordering, Ranking, or More/Less
 - Gotcha: even if used with Numbers it may be still a Nominal.
 - Example: colors, names, room numbers, ID numbers

137

Psychology 402 - Spring 2024 - Dr. Michael Diehr

Ordinal Scale

- Ordinal : ordering
 - first, second, third....
 - 1, 2, 3...
 - A, B, C...
- signifies Order, but can't assume distance between items is the same, e.g. the difference between an A and a B may be much different than a B and a C
- Example: Class Rank, Assignment Grade, Product Ratings

138

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Interval Scale

- Interval: specifies orders AND inter-item distance
 - -3, -2, -1, 0, 1, 2, 3.... 100, 105, 115
 - the difference between two numbers IS the same, e.g. 100 to 105 should be the same amount as 105 to 110
 - Does NOT have an absolute zero.
- Example: temperature in Degrees Fahrenheit

139

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Ratio Scale

- Ratio: specifies orders AND inter-item distance and has absolute zero
 - 0, 1, 2, 3.... 100, 105, 115
 - the difference between two numbers IS the same, e.g. 100 to 105 should be the same amount as 105 to 110
 - Does have an absolute zero.
- Example: temperature in Degrees Kelvin

140

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Measurement Scales

| | Magnitude | Equal Intervals | Absolute Zero |
|----------|-----------|-----------------|---------------|
| Nominal | | | |
| Ordinal | ✓ | | |
| Interval | ✓ | ✓ | |
| Ratio | ✓ | ✓ | ✓ |

141

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Scales: Practical Info

- Nominal Scale: common
 - common stats: Count, Frequency, Mode
- Ordinal Scale: less common
 - stats: specialized "nonparametric" techniques required
- Ratio and Interval: common
 - Often can be treated identically with same statistical techniques

142

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Basic Statistics

- Why use numbers?
 - Pros:
 - convenient, succinct
 - universal
 - well-defined, repeatable
 - Cons:
 - precision vs. accuracy
 - numerical fallacy

143

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Tabular Data

144

Table 1:

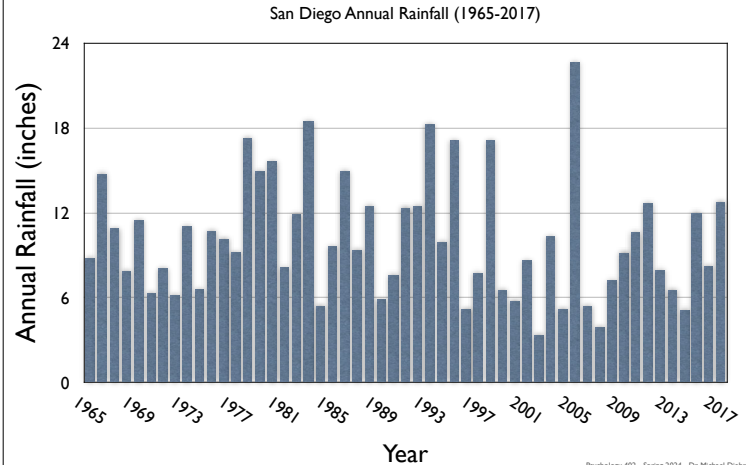
San Diego Annual Rainfall (in Inches) by Year

| Year | Rainfall (inches) |
|------|-------------------|
| 1965 | 8.81 |
| 1966 | 14.76 |
| 1967 | 10.86 |
| 1968 | 7.86 |
| 1969 | 11.48 |

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Data Distributions

145



Histogram

- Frequency Distribution
- Invented by Karl Pearson
- Shows data from *one* variable only
- Data is (often) collected into groups (“bins”)

146

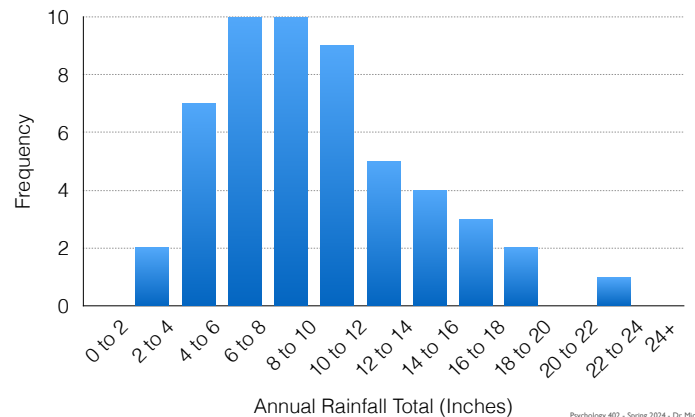
Psychology 402 - Spring 2024 - Dr. Michael Dohr

Histogram

148

Figure 1

Frequency Distribution of San Diego Annual Rainfall



Describing Distributions

- Why? Large lists are inconvenient. Reduce many data points to a few numbers.
- Issue: Reducing data (“Degrees of freedom”) : throws away data.
- We are modeling our data using a simplification.
- “All models are wrong, some models are useful”
- Simple vs. Simplistic?

149

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Descriptive Statistics

- Statistical Assumptions: When these are not met, weird things happen.
- Joe Smith is 6 feet tall, his child is 1 foot tall. Thus, the average height in the Smith household is 3.5 feet.
- If you are sitting in bar, and Bill Gates walks in, suddenly everyone in the bar is (on average) a multi-millionaire.

150

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Alternative Notations

- Square Root (x) $\text{sqrt}(X)$ \sqrt{X} $\sqrt[2]{X}$
- X-Squared X^2 X^{**2} X^2
- Sum(x) $X_1+X_2+X_3...$ $\sum_{i=1}^N x_i$ $\sum x$
- Mean M $\frac{\sum x}{N}$ \bar{X}

151

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Central Tendencies

- Values tend to cluster around a point.
- **Mean** : most common statistic, commonly referred to as the “average”. Formula $\sum X / N$
- **Mode**: the most common value in a set
 - rare to use in statistics
- **Median**: the middle-most value in a set
 - the value at which half are above and half are below. Aka the 50th percentile.

152

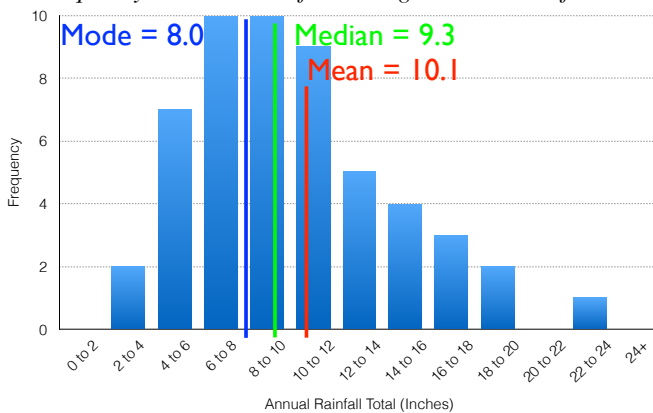
Psychology 402 - Spring 2024 - Dr. Michael Dohr

Histogram

153

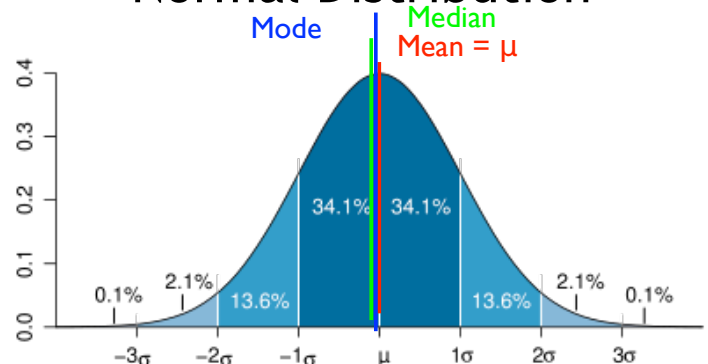
Figure 1

Frequency Distribution of San Diego Annual Rainfall



Psychology 402 - Spring 2024 - Dr. Michael Dohr

Normal Distribution

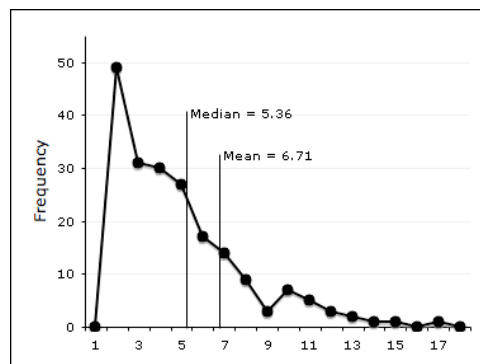


In a normal distribution, the mean, mode, and median are all the same

154

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Skewed Distribution

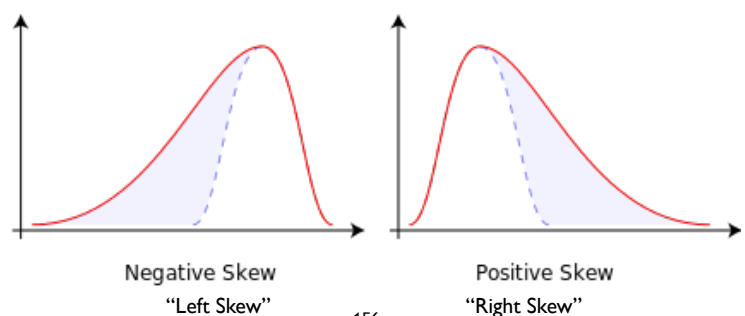


In a skewed distribution, the mean, mode, and median are all often different

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Skew

- negative skew : fatter tail on the left
- positive skew : fatter tail on the right



156

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Measures of Central Tendency 1

| | Description | Algorithm | Formula |
|---------------|-------------------------|--------------------------------|--|
| Mean | the “average” | sum values, divide by N | $\bar{x} = \frac{\sum_{i=1}^N x_i}{N}$ |
| Median | the “middle-most value” | sort values, find middle value | 50th percentile |
| Mode | the “most common” value | find most frequent value | ... |

157

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Measures of Central Tendency 2

| Behavior: | Normal Distribution | Skewed Distribution |
|---------------|---------------------|------------------------------|
| Mean | same | overly affected by outliers |
| Median | same | fairly resistant to outliers |
| Mode | same | resistant to outliers |

158

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Measures of Dispersion 1

- Compare each measured value to the average
- “for a typical value, how far away is it from the mean”
- “Difference score” or “residual” can be calculated as the difference between the actual score and the mean. In other words, $d_i = x_i - \bar{X}$
- Take the average (mean) of the difference scores.
- Average difference score = $\text{Sum}(d) / N$

160

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Average Difference Score

161

| | Score (x) | Mean (\bar{X}) | Difference $d = (x - \bar{X})$ |
|-------------|-----------|--------------------|--------------------------------|
| | 2 | 6 | -4 |
| | 3 | 6 | -3 |
| | 9 | 6 | 3 |
| | 11 | 6 | 5 |
| | 14 | 6 | 8 |
| | 1 | 6 | -5 |
| | 6 | 6 | 0 |
| | 4 | 6 | -2 |
| | 5 | 6 | -1 |
| | 5 | 6 | -1 |
| Sum | 60 | 60 | 0 |
| Mean | 6 | 6 | 0 |

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Sum of Residuals

- Given N samples of x : $x_1, x_2, x_3 \dots x_N$
- mean of x $\bar{x} = \frac{\sum_{i=1}^N x_i}{N}$
- residuals $d_i = x_i - \bar{x}$
- Sum of Residuals is always zero

$$\sum_{i=1}^N d_i = 0$$

162

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Sum of Residuals

- The “average difference score” score will *always* equal zero
- Solution:
 - Square the residuals *before* adding: removes the negative values.
 - “SSR” or Sum of Squared Residuals

163

Psychology 402 - Spring 2024 - Dr. Michael Dohr

SSR: Sum of Squared Residuals ¹⁶⁴

- Given N samples of X: $x_1, x_2, x_3 \dots x_N$
- mean of x
$$\bar{x} = \frac{\sum_{i=1}^N x_i}{N}$$
- residuals
$$d_i = x_i - \bar{x}$$
- Sum of Squared Residuals (SSR)

$$SSR = \sum_{i=1}^N (d_i)^2$$

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Problems with SSR

- SSR depends on units of measurement:
 - a meter is 1000 millimeters, so SSR will be $1000 \times 1000 =$ one million times higher when using meters vs. millimeters
- SSR depends on N (# of samples)
 - Doubling N will cause SSR to double (roughly)
- Therefore, SSR is hard to understand:
 - is SSR = 0.00342 high or low?
 - is SSR = 2343249 high or low?

165

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Remove the influence of N

- The Sum of a set of values depends on the number (N) of values:
 - $\sum_{i=1}^N x_i$
- Take the average (mean)
 - this divides by N
 - removes the influence of N

166

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Variance

- Problem: SSR depends on N
- Solution: Take the average of SSR to remove the influence of N
- The average of the squared residuals is called Variance (S^2)

167

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Variance

- Variance = SSR/N
- Variance = mean of squared residuals

$$S^2 = \frac{\sum_{i=1}^N (d_i)^2}{N}$$

$$S^2 = \frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}$$

168

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Problems with Variance

- Units are squared:
 - measuring height in meters?
variance is meters²
 - measuring # of cupcakes eaten?
variance is (# of cupcakes eaten)²
- Won't someone rid me of these meddlesome squared units?

169

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Standard Deviation

- Improving on Variance:
- The square root of Variance (S^2) gives S , which is called "Standard Deviation".
- Also abbreviated SD, StdDev or σ (Greek letter sigma), or sometimes just "S"
- SD : easier to understand because it's in the same units as your measurement.
- SD is a unique property of the normal distribution -- given a mean and a SD you have uniquely specified the distribution

170

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Standard Deviation

- SD = Square root of Variance

$$S = \sqrt{\frac{\sum_{i=1}^N (d_i)^2}{N}}$$

$$S = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N}}$$

171

Psychology 402 - Spring 2024 - Dr. Michael Dohr

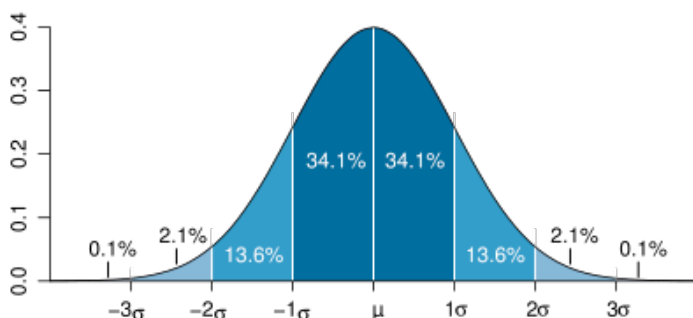
Standard Deviation

- can be thought of as the "average deviation"
- (but it's not literally average deviation, since we showed earlier the average difference score is always Zero)
- Technically:
 - (in a normal distribution) scores will be within plus or minus 1 SD about 68% of the time

172

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Normal Distribution



In a normal distribution, about 68.2% of values fall within ± 1 SD

173

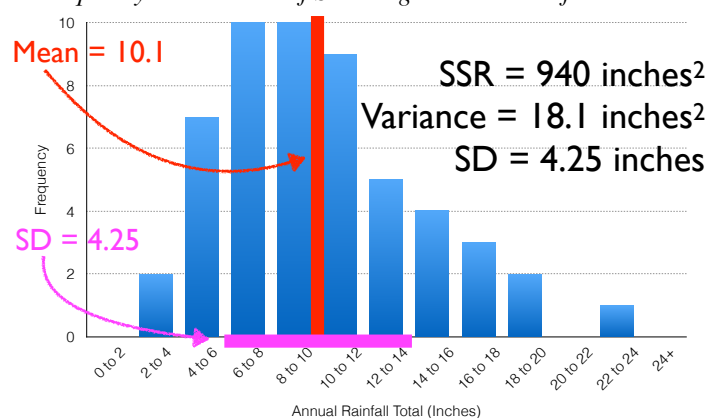
Psychology 402 - Spring 2024 - Dr. Michael Dohr

SSR, Variance and SD

174

Figure 1

Frequency Distribution of San Diego Annual Rainfall



Psychology 402 - Spring 2024 - Dr. Michael Dohr

Central Limit Theorem

- No matter the shape of the Population distribution, if you take enough (*) samples of the mean, the distribution of your samples of the mean will have a Normal distribution
- Central Limit Theorem Exercise (Javascript)
- This fact makes our life easy: Many statistics assume a normal distribution. The CLT provides us a normal distribution in most cases, even when the population data is skewed

175

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Exercise: normal distribution

- Roll one 10-sided die 10 times and record the results
- Prediction
 - Your Distribution: Uniform (flat)
 - Mean : 4.5
 - Class Distribution: ???
- hint: What is N? # die rolls, # of students?
- List and Graph results
- Does the distribution look normal?
 - if so, why?

176

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Exercise I: Die Rolls

| Trial # | X_i | M | $d = (X_i - M)$ | (residual) ² |
|---------|-------|-----|-----------------|-------------------------|
| 1 | 2 | 3.5 | -1.5 | 2.25 |
| 2 | 4 | 3.5 | 0.5 | 0.25 |
| 3 | 6 | 3.5 | 2.5 | 6.25 |
| 4 | 2 | 3.5 | -1.5 | 2.25 |
| Sum: | 14 | | | |

| N # of rolls | $M = \bar{X}$ | | Σ Residuals | Σ (residual ²) | $\frac{\Sigma (\text{residual}^2)}{N-1}$ | s^2 |
|-----------------|---------------|--|--------------------|-----------------------------------|--|-------|
| 4 | 3.5 | | 0.0 | 11.0 | 3.67 | 1.92 |

177

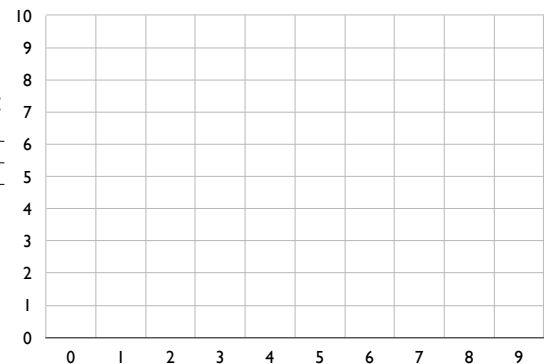
Psychology 402 - Spring 2024 - Dr. Michael Dohr

Title:

Figure 1

Blah de Blah Blah Blah

Y axis label:



X axis label:

Note:

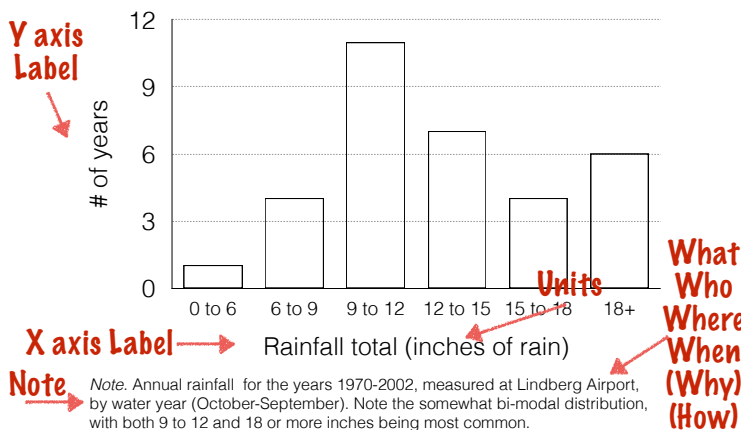
178

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Example of APA-7 style Histogram

Figure 1

Frequency Distribution of Annual Rainfall in San Diego



179

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Exercise: normal distribution 2

- Compute Mean (\bar{X}) - is it near 4.5?
- Compute residuals
- Compute sum of residuals -- do they add to zero?
- Compute squared residuals
- Compute Sum of squared residuals (SSR)
- Divide SSR by (N-1) - this is Variance or (S^2)
- Take square root of variance - this is S or Standard Deviation
- For this exercise, SD should be near 2.8

180

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Ch. 2 - Part 2

185

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Review

191

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Population vs. Sample

- Ideally, measure *everyone* to get the exact value (*Population parameter*)
- Practically, this is impossible.
- Take samples instead, and calculate the *Sample statistic*.
- The “Law of Large Numbers”, “Sampling Theory”, “Central Limit Theorem” makes life easier
- [Central Limit Theorem Exercise \(Javascript\)](#)
- Some formulas differ for *Population* vs. *Sample* (divide by N or divide by N-1 ?)

199

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Population v. Sample

| | Population | Sample |
|-----------------------|-------------------------|--------------------------------|
| Definition | the entire set of items | the actual subset you measured |
| Descriptives | “Parameters” | “Statistics” |
| Symbols | Greek | Roman |
| Mean | μ | \bar{x} |
| Std. Deviation | σ | S |
| Variance | σ^2 | S ² |
| <i>Divide by</i> | N | N-1 |

200

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Law of Large Numbers

- If you take enough* samples, the sample mean approaches the population mean.
- Example: a coin has two sides. If heads=1 and tails = 0, then the average expected result is exactly 50% Heads (0.5) in the long run.
- However, if you flip a coin just a few times, getting exactly 0.5 is not likely.
- The LLN states that you will if you take enough samples.

* what is “enough”? Rule of thumb : 100.

201

Psychology 402 - Spring 2024 - Dr. Michael Dohr

LLN Demonstration

- Law of Large Numbers
- [Demonstration with Coin Flips](#)

202

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Logical Fallacies

203

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Logical Arguments

- Logical arguments or inferences generally have several components:
 - Premises
 - Conclusions
- Example:
 - Premise: All English people are musicians
 - Premise: John Lennon was English
 - Conclusion: John Lennon was a musician

204

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Logical Arguments 2

- An Inference can be either Valid or Invalid -- this refers to the Structure of the argument (not the Facts themselves)
 - All A are B
All C are A
All C are B
- A Valid inference can still come to a false conclusion, and vice-versa

205

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Logical Fallacies

- A Logical Fallacy generally means that your inference is Invalid to begin with. In addition, your facts may or may not be true, but the flaw in reasoning has occurred before you even apply facts.
- Example: Affirming the consequent
- If P, then Q bank owners are rich
Q is true Bill Gates is rich
Therefore P Bill Gates owns a bank

206

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Biased Sample

- Every individual x that we have seen from sample X has characteristic Z
Therefore ALL X have characteristic Z
- Every student I talk to in this class is interested in Psychology
Therefore, ALL students are interested in Psychology

208

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Nominal and Numeric

- Nominal Fallacy: The tendency to believe that something has a name or identification, it exists or has special meaning.
“I am sleepy” vs. “I am suffering from activity-induced-rest-reduction-performance-impairment syndrome”
- Numerical Fallacy: belief that something has been measured and assigned a number, it actually exists. “I’m really sad” vs. “I scored a 32 on the Beck Depression Inventory”

209

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Reification Fallacy

- To Reify - to make something more concrete or real
- Examples:
 - “An A student”
 - “High IQ”
 - “Top of the class”
 - “A F Grade”

210

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Ranking Fallacy

- Reducing a complex phenomenon (e.g. intelligence), giving it a single number (reification) and then ordering based on that number
- Examples:
 - A IQ of 93 is better than an IQ of 90
 - An income of \$50,000 is better than \$45,000

211

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Correlation = Causation

212

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Other Fallacies

- Begging the question -- circular argument
- Post hoc ergo propter hoc (*after* this, therefore *because* of this)
- Appeal to Authority
- False Dilemma (Black & White thinking)

214

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Significant Figures

- “digits of precision” or “sig. fig.”
- 1.3 has 2 sig. fig.
- 1.3455 has 5 sig. fig.
- More significant figures → more precision

215

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Precision vs. Accuracy

- Precision : the level of detail a measurement is made with, often specified with an error-range
 - “about 6 feet plus or minus 1 foot” vs. “6 foot 11 inches plus or minus 1 inch”
- Accuracy: how close the measured value is to the actual value, does it “hit the target”
- Think arrow vs. shotgun
- A number can be precise and accurate, precise but inaccurate, or accurate but imprecise.

216

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Precision Fallacy

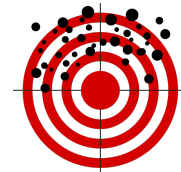
- A number that is *precise* may seem to be *accurate* when it is not
- A measurement that is *reliable* may seem to have *validity* when it does not

217

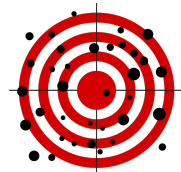
Psychology 402 - Spring 2024 - Dr. Michael Dohr

218 Precision vs. Accuracy

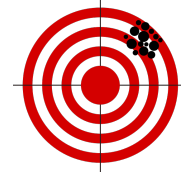
- Target shooting analogy
- Similar to Reliability vs. Validity



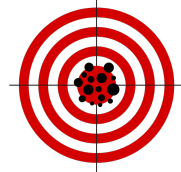
Unreliable & Unvalid



Unreliable, But Valid



Reliable, Not Valid



Both Reliable & Valid

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Fallacies re: Probability

- Classical
- Gambler's Fallacy
- Bayesian Reasoning

219

Psychology 402 - Spring 2024 - Dr. Michael Dohr

9 Heads in a row

- You are flipping a coin, and get 9 heads in a row
H H H H H H H H H
- What is the % chance the next flip will be a H ?
- Three common answers:
 - 50/50
 - more likely Heads
 - more likely Tails

220

Psychology 402 - Spring 2024 - Dr. Michael Dohr

9 Heads: Classical Inference

- Coin flips are independent 50/50 events, therefore 50% : Logical/Statistical
- This is the **correct** answer *for a fair coin*

221

Psychology 402 - Spring 2024 - Dr. Michael Dohr

9 Heads: Gambler's Fallacy

- Coin flips are independent 50/50 events, but we just saw 9/10 heads, therefore a Tail is "due"
- This is the "Gambler's Fallacy" and one reason Casinos make tons of money. The reasoning is faulty.
- Note: when dealing with draws w/o replacement, this logic is **correct**. For example, a single-card blackjack deck -- if no face cards have come up after 30 cards, then face cards are due

222

Psychology 402 - Spring 2024 - Dr. Michael Dohr

9 Heads: Bayesian Statistics

- Coin flips are supposed to be 50/50 events, but we just saw 9/10 heads, therefore the data is telling us that perhaps this is not a fair coin.
- Bayes' theorem suggests you evaluate the prior probabilities in determining future behavior
- In this case, you'd conclude that Head is more likely on the next flip

223

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Cognitive Biases of Discrimination

- Which cognitive biases (logical fallacies) are involved in racism, sexism and other bigoted beliefs?

224

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Review - History

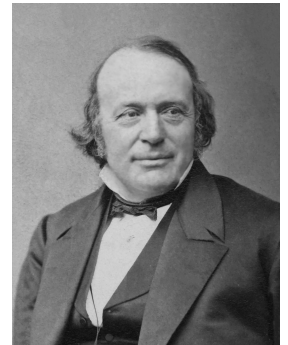
- Themes
 - 18th-19th century
 - 19th-20th century
- Theories of Human Development
 - Creationism
 - Polygenism
 - Evolution
 - Genetics
- Controversy
 - IQ testing of various groups

225

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Louis Agassiz

- Swiss-born, European-trained biologist / geologist
- Came to Harvard in 1847
- Creationist -> Polygenist
- Taxonomist
- Resisted Darwin's theory of Evolution
- d. 1873

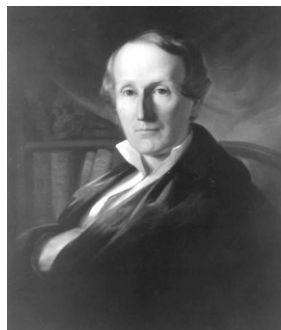


226

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Review: Samuel George Morton

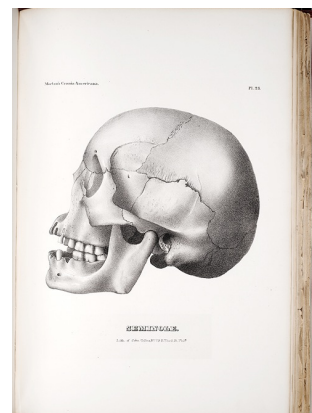
- Theory of Polygenism
 - Humans are composed of different species, created by god
- Craniometry
- Biological Determinism
- "Scientific Racism"
- The "American School"
- d. 1851



227

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Crania Americana



Samuel George Morton
1839

229

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Morton's Data as printed

| Race | N | Cranial Volume Mean |
|-----------|-----|---------------------|
| Caucasian | 52 | 87 |
| Mongolian | 10 | 83 |
| American | 144 | 82 |
| Malay | 18 | 81 |
| Ethiopian | 29 | 78 |

232

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Data, corrected

| Race | Mean (Morton) | Mean (corrected) |
|-----------|---------------|------------------|
| Caucasian | 87 | 87 |
| Mongolian | 83 | 87 |
| American | 82 | 86 |
| Malay | 81 | 85 |
| Ethiopian | 78 | 83 |

233

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Seed vs. Shot

| Race | Difference (seed - shot) |
|-----------|--------------------------|
| Caucasian | 1.8 |
| Mongolian | n/a |
| American | 2.2 |
| Malay | n/a |
| Ethiopian | 5.4 |

235

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Morton's errors

- Fundamental arithmetic errors
- Data selection errors
- Failure to measure or control for external variables (biological sex, body size, etc.)
- Basic Statistical errors (averaging measurements from unequal size subgroups)
- The racist thumb press?
- Is he a liar? Conscious or subconscious?

236

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Morton's Model

237

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Internal vs. External Validity

- Internal Validity - how did it work?
 - were the methods good
 - did the IV cause the DV
- External Validity - what does it mean?
 - does skull size indicate IQ?
 - does IQ indicate personal worth?

238

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Comparing Scores

- Compare a single score to the population
- One way: difference scores
- Problem: Is a difference of “3” big or little?
On a 100 point test it’s not very large, but on a 10 point test it’s the difference between an A and a C

239

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Comparing Scores

- Desire a system independent of the raw score units (just like letter grades)
- Two methods:
 - Ranks & Percentile Ranks...
 - Standard Scores...

240

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Ranks, Percentiles

- Given a distribution of scores, and a single score
- **Rank** = the item # of the single score when sorted high to low
- **Percentile Rank** = the % of scores which are lower than the given score
- **Percentile** = the score at which a given percent of scores are below a given score
- Note: “**Percentile**” often used informally to mean “**Percentile Rank**”

241

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Rank & Percentile

- Coronavirus Deaths
- Total deaths, per million people, as of September 2020
- Sort low to high

| Country | Score |
|------------|-------|
| Mozambique | 0.9 |
| China | 3.0 |
| Ethiopia | 8.0 |
| Japan | 11.0 |
| Zambia | 16.0 |
| Colombia | 424.0 |
| France | 471.0 |
| Sweden | 577.0 |
| USA | 584.0 |
| Bolivia | 599.0 |

243

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Rank & Percentile

- Determine Rank #

| Country | Score | Rank |
|------------|-------|------|
| Mozambique | 0.9 | 1 |
| China | 3.0 | 2 |
| Ethiopia | 8.0 | 3 |
| Japan | 11.0 | 4 |
| Zambia | 16.0 | 5 |
| Colombia | 424.0 | 6 |
| France | 471.0 | 7 |
| Sweden | 577.0 | 8 |
| USA | 584.0 | 9 |
| Bolivia | 599.0 | 10 |

244

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Percentile Rank

Percentile Rank = # of cases with worse value divided by # of cases

e.g. France is 7th of 10 (it has 3 cases with worse values)
 $3 / 10 = 30\%$
 percentile rank

| Country | Score | Rank | %ile Rank |
|------------|-------|------|-----------|
| Mozambique | 0.9 | 1 | 90 |
| China | 3.0 | 2 | 80 |
| Ethiopia | 8.0 | 3 | 70 |
| Japan | 11.0 | 4 | 60 |
| Zambia | 16.0 | 5 | 50 |
| Colombia | 424.0 | 6 | 40 |
| France | 471.0 | 7 | 30 |
| Sweden | 577.0 | 8 | 20 |
| USA | 584.0 | 9 | 10 |
| Bolivia | 599.0 | 10 | 0 |

245

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Standard Scores 2

- Use the mean and standard deviation as points of reference.
- Standard score : distance from the mean, scaled by standard deviation
- Not affected by raw score units.
- Different standard scores mean the same thing, but are expressed differently.
 - just like how 1.0 and 100% mean the same thing
- Unfortunately, there are several different Standard Score systems!

247

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Z-score

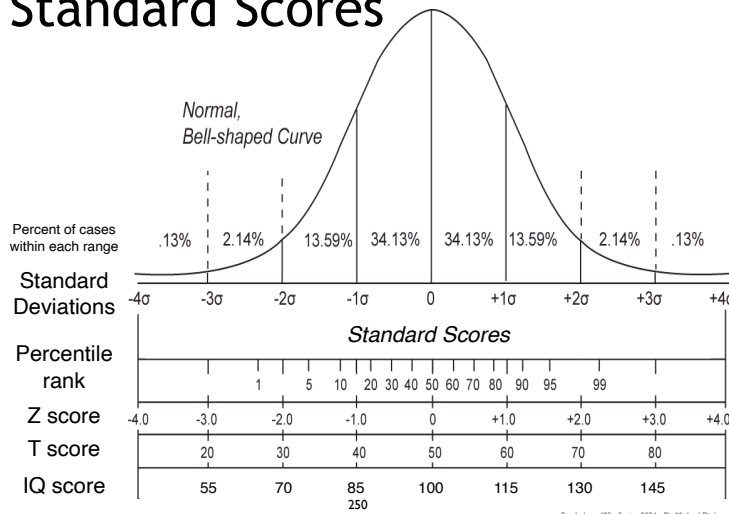
- A Z score is the # of standard deviations above (+) or below (-) the mean of a single measurement.
- Algorithm: given a single score (X_i), subtract the mean M , divide by the standard deviation S
- Formula
 - $Z = (X - M) / SD$

$$Z_i = \frac{X_i - \bar{X}}{S}$$

249

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Standard Scores



Psychology 402 - Spring 2024 - Dr. Michael Dohr

Standard Scores: Z, T, IQ

| | Z scores | T scores | IQ scores |
|-----------------------|----------|-----------|------------|
| Mean | 0 | 50 | 100 |
| SD | 1 | 10 | 15 |
| Example: top 3% | | | |
| Example: top 1% | | | |
| Formula: from Z Score | Z | (Z*10)+50 | (Z*15)+100 |

251

Psychology 402 - Spring 2024 - Dr. Michael Dohr

| z-Score ($(x - \bar{x}) / s$) | T-Score $10z + 50$ | Wechsler IQ ($15z + 100$) | Percentile Rank |
|------------------------------------|-----------------------|--------------------------------|-----------------|
| 3.0 | 80 | 145 | 99.9 |
| 2.9 | 79 | 144 | 99.8 |
| 2.8 | 78 | 142 | 99.7 |
| 2.7 | 77 | 141 | 99.6 |
| 2.6 | 76 | 139 | 99.5 |
| 2.5 | 75 | 138 | 99.4 |
| 2.4 | 74 | 136 | 99.2 |
| 2.3 | 73 | 135 | 98.9 |
| 2.2 | 72 | 133 | 98.6 |
| 2.1 | 71 | 132 | 98.2 |
| 2.0 | 70 | 130 | 97.7 |
| 1.9 | 69 | 129 | 97.1 |

252

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Norms 1

- Standard Scores provide us with a way of describing how a particular score relates to others in the population.
- Describing how an individual score relates to the population, which we assume are “normal”.
- Terms “normative data” and “norms”
- Key questions: What is the normative group? What features or factors of the group may affect scores?

253

Psychology 402 - Spring 2024 - Dr. Michael Dohr

Z-score Exercise

- This is for practice, not graded for points
- PDF is on class website