

# Ch. 4: Reliability

Copyright © 2025 Michael Diehr  
All Rights Reserved  
For use only by students enrolled  
in my sections of Psyc 402  
through the end of the semester.  
May not be posted, shared or uploaded  
online without permission.

570

Psychology 402 - Spring 2025 - Dr. Michael Diehr

571

Psychology 402 - Fall 2024 - Dr. Michael Diehr

## Reliability

- Constructs & Measurement
- History
- Classical Test Score Theory
- Four Kinds of Reliability
- Standard Error of Measurement
- Increasing Reliability

590

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Constructs & Measurement

- Psychology as “soft science”
- Construct
  - exists but can’t be directly measured
  - examples
- Measurement
  - “true value” - intelligence
  - measured or *observed* value (e.g. score on a IQ test)
  - discrepancy - “error”
  - How to conceptualize *error*?

591

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## History 1

- 1896 - Karl Pearson - product-moment correlation (for continuous variables)
- 1904 - Charles Spearman - “*The proof and measurement of association between two things*” - *Rho* - correlation for Ordinal variables

592

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## History

- Pearson, Spearman, Thorndike (1900-1907)
  - Basic reliability theory
- Kuder, Richardson (1937), Cronbach (1989)
  - Reliability coefficients
- Bartholomew & Knott (1990s)
  - Latent variable theory
- Drasgow et al (late 1990s)
  - Item Response Theory (IRT)

593

Psychology 402 - Spring 2025 - Dr. Michael Diehr

# Classical Test-Score Theory

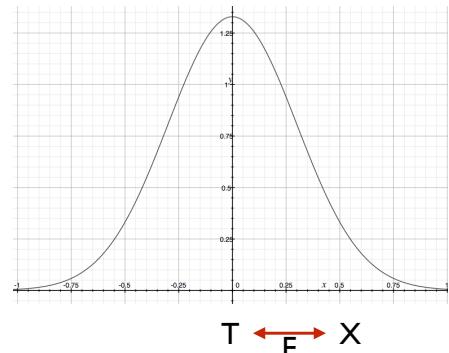
595

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## 596 Classical Test-Score Theory

- T = True Score
- X = Observed
- E = Error

- X = T + E
- E = X - T



Psychology 402 - Spring 2015 - Dr. Michael Diehr

# Classical Test-Score Theory

- True score (T) : the “actual” score that exists
- Observed score (X) : score as measured by a test
- Error (E) : difference between Observed and True score
- $X = T + E$
- $E = X - T$
- Assumptions: True scores have no variability. Errors are random (e.g. a normal distribution with mean of zero)

597

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Classical Test-Score Theory: Reliability

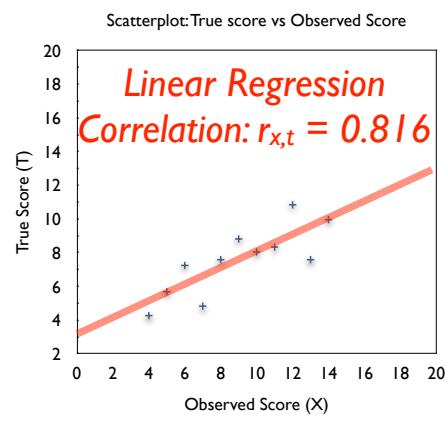
- Reliability = correlation between Observed score and True score
- $R_{X,T}$

598

Psychology 402 - Spring 2015 - Dr. Michael Diehr

# Classical Test Score Theory

X	T
10	8.04
8	7.58
13	7.58
9	8.81
11	8.33
14	9.96
6	7.24
4	4.26
12	10.84
7	4.82
5	5.68



599

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Models of Reliability

- Most reliability measures are Correlation coefficients
- Alternate definition: Reliability is the ratio of the variance of True scores to the variance of the Observed scores
  - $\rho^2_{XT} = \frac{\sigma^2_T}{\sigma^2_X}$
- Or, it's the “Signal to Noise” ratio
  - $\rho^2_{XT} = \frac{\sigma^2_T}{\sigma^2_T + \sigma^2_E}$
- A test with reliability of  $r^2=0.40$  means that 40% of variation in test scores is due to variation in the “true” score, and 60% of variation is random or chance factors.

600

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Sources of Error

- “Error” is considered the difference between True score and Observed score
- Where does Error arise?
  - Measurement errors
  - Change in True score
  - Sampling issues
  - Observer effects
  - etc...

601

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Measuring Reliability in Practice

- Since True score is hidden, can't use the direct formula:  $R_{X,T}$
- Instead
  - think about sources of error
  - practical methods
  - *estimate* reliability

602

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Test-Retest Reliability

- Test-Retest
  - administer test, delay for interval, administer test again
  - compute correlation between two administrations
  - same subjects, exact same test, two administrations

603

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Test-Retest Reliability

- Pros
  - easy for experimenter to do
- Cons
  - what causes error?
  - short testing interval → practice effects
  - long testing interval → change in true score over time
  - subjects have to take test 2x

604

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Parallel Forms Reliability

- Also called “alternate” or “equivalent” forms
  - Item Sampling
  - administer two versions of the test to same subjects (can have zero delay)
  - compute correlation between two scores
  - same subjects, different test forms, two administrations
- Pros: more rigorous method of determining reliability
- Cons: more work: experimenter must make a second test, subjects have to take 2 tests

605

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Internal Consistency Reliability

606

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Internal Consistency Reliability

- Give single test, calculate internal consistency of various subsets of items
- Only one test, one administration, same group of subjects
- Older methods:
  - Split half method
  - Spearman-Brown formula
  - KR20 formula
  - average of all possible Split Halves
  - can only handle right/wrong scoring
  - newer methods are better...

607

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Internal Consistency Reliability

- New: **Cronbach's Alpha ( $\alpha$ )**
  - estimates a lower bound for reliability
  - does not require right/wrong scoring
    - can be used with Likert scales
  - $\alpha \geq .90$  is good
  - $\alpha \geq .80$  is ok
  - $\alpha$  between  $.70 - .80$  is borderline
  - $\alpha < .70$  is bad

608

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Inter-Rater Reliability

- Observational data differs from self-report data
- Though behavioral rating systems attempt to be precise, errors occur (e.g. did the child fall down? or were they pushed?)
- We must consider the reliability of different observers ("raters")
- **Cohen's Kappa**
  - ranges from -1 to +1
  - "poor"  $< .40$
  - "good"  $.40$  to  $.75$
  - "excellent"  $> .75$

609

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Reliability: errors & methods

	Description	Name	Statistic
<b>Time Sampling</b>	1 test given two times	test-retest reliability	correlation between scores at two times
<b>Item Sampling</b>	2 different tests given once	Alternate or Parallel forms	correlation between scores on 2 versions
<b>Internal Consistency</b>	One test, multiple items	Split Half or internal reliability	Cronbach's Alpha
<b>Observer Differences</b>	One test w/ 2+ observers	inter-observer reliability	Kappa

610

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Quiz: What kind of Reliability?

Procedure	Source of error?	Reliability?
Olympic judges giving consistent scores for a gymnastics performance		
Correlation between your IQ test score taken at age 12 and again at age 13		
Correlation between scores on 2 versions of the midterm (assuming each student takes both versions)		
Correlation between student scores on questions 1-25 vs 26-50 of the midterm.		

612

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Summary

- Reliability
  - how consistent measured scores are
- Error
  - $E = X - T$
- What kind of Error?
  - test-retest, item sampling, internal consistency, observer-differences

614

Psychology 402 - Spring 2025 - Dr. Michael Diehr

## Standard Error of Measurement

- “How close is this test score to the true score”
- If we know the Reliability ( $r$ ) of the test, we can estimate the likely range of true scores
- Given
  - $S$  = std dev of measured scores
  - $r$  = reliability coefficient of test

$$SEM = S\sqrt{1 - r}$$

$$\sigma_{meas}$$

615

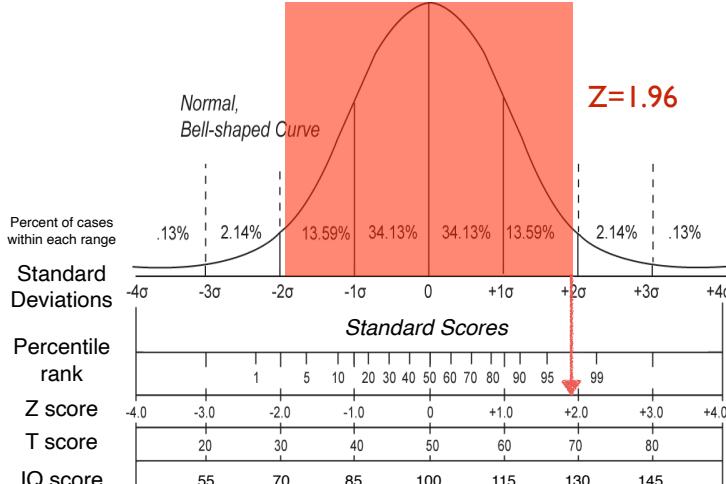
Psychology 402 - Spring 2015 - Dr. Michael Diehr

## SEM example: IQ

- Example: a person scored 106 on an IQ test, that has a reliability of 0.89. What is the 95% confidence interval of their true score
- $S = 14$
- $r = 0.89$
- $SEM = S\sqrt{1 - r}$
- $SEM = 14\sqrt{1 - 0.89}$
- $SEM = 4.64$
- Next, compute a confidence interval

616

Psychology 402 - Spring 2015 - Dr. Michael Diehr



617

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Confidence Interval

- “How likely is a true score to fall within a range”
- $Z$  = z-score associated with % range
- Confidence interval =  $Z * SEM$
- Example:
  - 95% confidence interval :  $Z = 1.96$
  - $SEM = 4.64$
  - $1.96 * 4.64 = 9.1$
  - 95% CI =  $\pm 9.1$  points
  - Range =  $X \pm CI$
  - $106 \pm 9.1 = \text{range from } 96.9 \dots 115.1$

618

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## SEM Exercise

- This is for practice, not turned in, not scored for points.

619

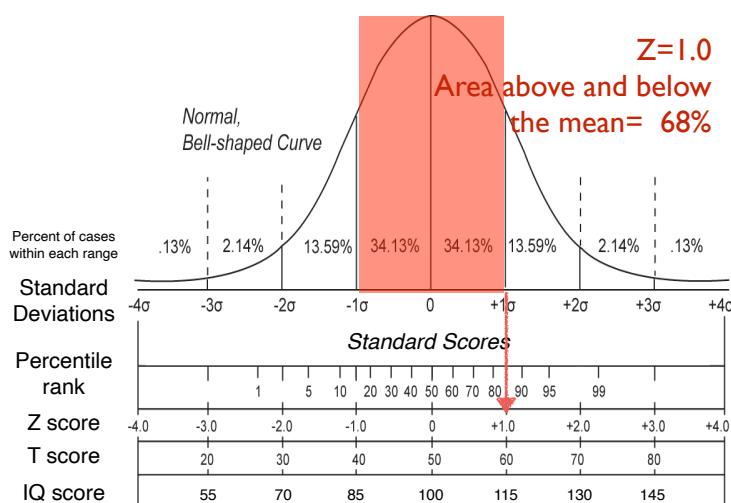
Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Common Z scores & Confidence Levels

Z Score	Area above mean	Area above + below Mean	Proportion as %
0.00	0.000		0%
0.13	0.051		
0.67	0.249		
1.00	0.341	0.682	68%
1.64	0.449		
1.96	0.475		95%
2.57	0.495		

620

Psychology 402 - Spring 2015 - Dr. Michael Diehr



621

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## How reliable?

- $r = .70$  or  $.80$  or higher is often considered “good enough” for much research
- $r > .90$  is very good
  - may not be worth effort to go higher
- Some real-world tests have  $r > 0.9$ 
  - example: modern IQ tests

622

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Increasing Reliability

623

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Increasing Reliability

- Increase  $N$  (number of questions, items or tests)...
- Focus on common characteristic...
- Other methods (covered later)
  - Use **Item Analysis** (“discriminability analysis”) to find items that best measure a single characteristic
  - Use **Factor Analysis** to determine sub-characteristics of a single test

624

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Increase N

- $N$  = number of questions or items or tests
- Formula: increase  $N$  to increase reliability
- $N_d = r_d (1 - r_o) / r_o (1 - r_d)$   
 $N_d$  = new  $N$  (times old  $N$ )  
 $r_d$  = desired level of reliability  
 $r_o$  = observed level of reliability

625

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Increase N - Examples

- Example 1
  - 20-item test has reliability of  $r=.87$
  - We desire  $r = .95$
  - $N_d = 2.82$ 
    - new  $N$  is  $2.82 \times 20 = 56$  items
- Example 2
  - Your 40-item test has reliability of  $.50$
  - We desire  $r=.90$
  - $N_d = 9.0$ 
    - new  $N$  is  $9 \times 40 = 360$  items

626

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Focus Test

- Reliability increases as a test focuses on a single concept or characteristic (“construct”)
- Trying to capture multiple concepts in a single test reduces reliability
- Methods:
  - Informal – remove items with poor face validity (chapter 5)
- Statistical:
  - Discriminability Analysis (chapter 6)
  - Factor Analysis (chapter 13)

627

Psychology 402 - Spring 2015 - Dr. Michael Diehr

## Reliability Summary

- Measurement Error occurs in all fields -- Psychology focuses on it
- Kind of Reliability : *where* the error came from
- Improving Reliability: more items, focusing test, discriminability, factor analysis
- Reliability is useful: calculate SEM to get Confidence Intervals
- Reliability is not Validity: Reliable tests aren't automatically valid
- A reliable test *might* be valid

628

Psychology 402 - Spring 2015 - Dr. Michael Diehr